

Section 12.4 Measures of Dispersion

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Measures of Dispersion indicate the extent to which values are spread around a central value such as mean.

-Examples: Interquartile Range, Range, Mean Deviation, Variance, and Standard Deviation.

Range and IQR are not very reliable to look at because they only use two data values.

-Write the formulas down in your notes from today

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Mean Deviation

-gives the average (mean) amount that the values in a data set differ from the mean.

Definition: the mean deviation of x_1, x_2, \dots, x_n is the mean of the absolute values of the differences between the values and the mean, \bar{x} .

$$\text{mean deviation} = \frac{1}{n} \sum_{i=1}^n |x_i - \bar{x}|$$

\sum -symbol called the sum

n- value of the data which you are trying to find the mean deviation for

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The table lists student's test scores in History. Find the range and mean deviation for the test scores.

History
85
91
96
85
93

Range:
High - Low
96 - 85 = 11

To find Mean Deviation:

-1. Find the mean (add them up and divide by the total):

$$\bar{x} = 90$$

-2. Make a table to find the absolute values of the differences from the mean.

x_i	$ x_i - \bar{x} $
85	$ 85 - 90 = 5$
91	$ 91 - 90 = 1$
96	$ 96 - 90 = 6$
85	$ 85 - 90 = 5$
93	$ 93 - 90 = 3$
Total:	20

(absolute value of the difference with the mean)

$$\frac{20}{5}$$

Divide the total by n (how many values):

$$\text{Mean Deviation} = 4$$

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Variance and Standard Deviation:

-If a data set has n values, and a mean of \bar{x} , then the variance and standard deviation are:

①
variance: $\sigma^2 = \frac{1}{n} \sum_{i=1}^n (x_i - \bar{x})^2$

②
Standard Deviation: $\sigma = \sqrt{\sigma^2}$

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Find the Standard Deviation and Variance from the test scores example. $\bar{x} = 90$

History	x_i	$x_i - \bar{x}$	$(x_i - \bar{x})^2$
85	85	$85 - 90 = -5$	$(-5)^2 = 25$
91	91	$91 - 90 = 1$	$1^2 = 1$
96	96	$96 - 90 = 6$	$6^2 = 36$
85	85	$85 - 90 = -5$	$(-5)^2 = 25$
93	93	$93 - 90 = 3$	$3^2 = 9$
Total:		X	96

To find Variance: $\frac{\text{total}}{n} = \frac{96}{5} = 19.2$

Standard Deviation: $\sqrt{\text{variance}} = 4.38$

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Hwk: pg. 796 - 797
6 - 20 every 4th, 27 - 28

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