

Journal Entry:

-Can the graph of a polynomial function be a straight line? If so, give an example of the function and show a graph of it.

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Section 5-2 Polynomials, Linear Factors and Zeros

Students will be able to:

- analyze the factored form of a polynomial
- write a polynomial function from its zeros

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Zeros of a function:

If $P(x) = 0$, all solutions are the zeros of the function.

Finding the zeros of the function will help you factor the polynomial, graph the function and solve the related polynomial equation.

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Solve by finding zeros (Chapter 4)

$$0 = x^2 - 6x + 5$$

$$0 = (x-5)(x-1)$$

$$x = 5, 1$$

We used the Zero Product Property to solve. You can use the same method to solve polynomials.

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Factor:

$$x^3 - x^2 - 12x$$

$$x(x^2 - x - 12)$$

$$x(x+3)(x-4)$$

$$x = 0, -3, 4$$

$$\begin{array}{cc} 1 & 12 \\ 2 & 6 \\ \hline 3 & 4 \end{array}$$

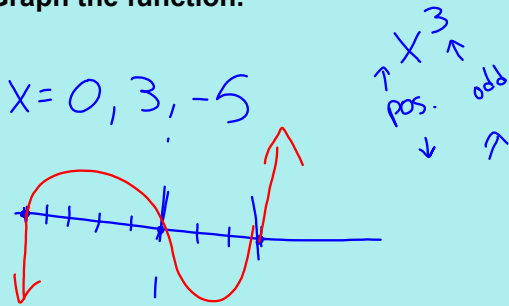
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The following are all true for the polynomial function $P(x)$ and a real number b

- $x - b$ is a factor of $P(x)$
- b is a root (or solution) of $P(x) = 0$
- b is an x -intercept of the graph of $y = P(x)$

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What are the zeros of $y = x(x - 3)(x + 5)$?
Graph the function.



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The factor theorem describes the relationship between the linear factors of a polynomial and the zeros of a polynomial.

Factor Theorem- the expression $x - a$ is a factor of a polynomial if and only if the value a is a zero of the related polynomial function.

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What is a cubic polynomial function with zeros $3, 3,$ and -3 ?

$$y = (x-3)(x-3)(x+3)$$

$$y = (x^2 - 6x + 9)(x+3)$$

$$y = x^3 - 6x^2 + 9x + 3x^2 - 18x + 27$$

$$y = x^3 - 3x^2 - 9x + 27$$

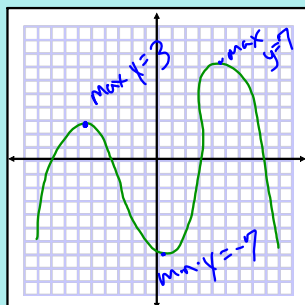
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$$f(x) = (x - 1)(x - 1)(x + 3)$$

Since $x - 1$ appears twice, we can say that 1 (the zero or solution of the factor $x - 1$) is a zero of multiplicity 2.

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If the graph of a polynomial has several turns, the function has a relative minimum and/or a relative maximum.



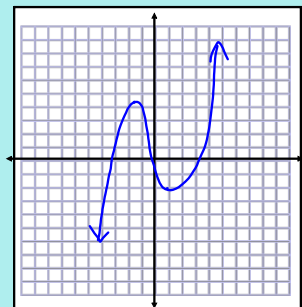
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What are the relative min and/or max of the following?

$$f(x) = 3x^3 + x^2 - 5x$$

$$\text{max} : 3.15 = y$$

$$\text{min} : -2 = y$$



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Hwk: pg. 293 - 294
#8 - 36 (4th), 38, 40, 44,
48, 54, 56

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