

Section 6-4
Rational Exponents

Students will be able to simplify expressions with rational exponents.

Aug 18-2:52 PM

$\sqrt{25}$ can be written as $25^{\frac{1}{2}}$

How would you write $\sqrt[4]{16}$ as a rational exponent?

$16^{\frac{1}{4}}$

Aug 18-2:52 PM

We can also write expressions that have rational exponents in radical form to simplify them.

$\sqrt[3]{8^{\frac{2}{3}}}$ can be written in two different ways

$\sqrt[3]{8^2} = \sqrt[3]{64} = 4$

$(\sqrt[3]{8})^2 = 2^2 = 4$

Aug 18-2:52 PM

Simplify:

$7^{\frac{1}{2}} \cdot 7^{\frac{1}{2}}$

$7^1 = 7$

$\sqrt{7} \cdot \sqrt{7} = \sqrt{49}$

Aug 18-2:52 PM

Simplify:

$5^{\frac{1}{4}} \cdot 125^{\frac{1}{4}}$

$5^{\frac{1}{4}} \cdot 5^{\frac{3}{4}} = 5^1 = 5$

Feb 11-3:31 PM

Write the following in radical form.

$5x^{\frac{1}{3}}$ = $5\sqrt[3]{x}$

8
27
64

$(54y)^{\frac{2}{3}}$

$\sqrt[3]{(54y)^2} = \sqrt[3]{\frac{2916y^2}{27 \cdot 108}} = 3\sqrt[3]{\frac{108y^2}{108}} = 3\sqrt[3]{y^2}$

$y^{-3.5}$

$y^{-\frac{7}{2}} = \frac{1}{y^{\frac{7}{2}}} = \frac{1}{\sqrt[2]{y^7}} = \frac{1}{\sqrt[2]{y^6 y}} = \frac{1}{y^3 \sqrt{y}}$

$\frac{\sqrt{y}}{y^4}$

Aug 18-2:52 PM

Converting to Exponential Form

Write in exponential form:

$$\sqrt[3]{b^3} = b^{3/3}$$

$$\sqrt[3]{27d^5} = (27d^5)^{1/3} = 3d^{5/3}$$

Aug 18-2:52 PM

Simplify:

$$\sqrt[4]{3} \sqrt[4]{3} = 3^{1/4} \cdot 3^{1/4} = 3^{2/4} = \sqrt[2]{27}$$

$$\frac{\sqrt{x^3}}{\sqrt[3]{x^2}} = \frac{(x^3)^{1/2}}{x^{2/3}} = \frac{x^{3/2}}{x^{2/3}} = x^{5/6}$$

Aug 18-2:52 PM

What is each number in simplest form?

$$32^{-3/5} = \frac{1}{32^{3/5}} = \frac{1}{(2^5)^{3/5}} = \frac{1}{2^{15/5}} = \frac{1}{2^3} = \frac{1}{8}$$

$$16^{3/4} = (2^4)^{3/4} = 2^{12/4} = 2^3 = 8$$

Aug 18-2:52 PM

To write an expression with rational exponents in simplest form, write every exponent as a positive number.

Write in simplest form:

$$(8x^{15})^{-1/3} = \frac{1}{(8x^{15})^{1/3}} = \frac{1}{8^{1/3} x^5} = \frac{1}{2x^5}$$

$$(9x^{1/2})^{3/2}$$

Aug 18-2:52 PM

Hwk: pg. 386-387
#10 - 64 (4th), 70, 76,
80 - 86 evens

Aug 18-2:52 PM

Aug 18-2:52 PM



Aug 18-2:52 PM