

**Section 7-6  
Natural Logarithms**

Students will be able to:  
 -evaluate and simplify natural log expressions  
 -solve equations using natural logs

Aug 18-2:52 PM

We said that the natural exponential function has a base e.

$$y = e^x$$

The inverse of this function is the natural logarithm

$$y = \log_e x \text{ or } y = \ln x$$

Aug 18-2:52 PM

What is  $\ln 7 + 2 \ln 5$  written as a single natural log?

$$\begin{aligned} \ln 7 + 2 \ln 5 & \\ \ln 7 + \ln 5^2 & \\ \ln 7(25) &= \ln 175 \end{aligned}$$

Aug 18-2:52 PM

The inverse relationship will be useful when solving natural log equations.

Solve:

$$\begin{aligned} \ln(3x + 5)^2 &= 4 & -4.13 &= \frac{-12.389}{3} = \frac{3x}{3} \\ \sqrt{e^4} &= \sqrt{(3x+5)^2} & .796 &= \frac{2.389}{3} = \frac{3x}{3} \\ \pm \sqrt{e^4} &= 3x+5 \\ \pm 7.389 &= 3x+5 \end{aligned}$$

Aug 18-2:52 PM

Solve:

$$e^{3x} + 5 = 15$$

$$\leftarrow \ln e^{3x} = \ln 10$$

$$\frac{3x}{3} \ln e = \frac{\ln 10}{3} \approx .767$$

Aug 18-2:52 PM

pg. 481

#15.  $\frac{1}{3}(\ln x + \ln y) - 4 \ln z$

$$\frac{1}{3}(\ln xy) - \ln z^4$$

$$\ln(xy)^{1/3} - \ln z^4$$

$$\ln \frac{(xy)^{1/3}}{z^4} = \ln \sqrt[3]{\frac{xy}{z^4}}$$

Aug 18-2:52 PM

Solve:

#24.  $\ln \frac{x-1}{2} = 4$

$$2e^4 = \frac{x-1}{2} + 1$$

$$x = 2e^4 + 1 \approx 110.16$$

Aug 18-2:52 PM

Solve:

#33.  $e^{x+1} = 30$

$$x+1 = \ln 30$$

~~$$x = \ln 30 - 1$$~~

$$\ln 30 = x+1$$

$$\ln 30 - 1 = x$$

$$\approx 2.401$$

Aug 18-2:52 PM

Simplify:

#50.  $\ln e^3$

3

Aug 18-2:52 PM

Hwk: pg. 481 - 482  
 #12 - 36 (4th), 38,  
 42 - 50 evens, 55, 56, 58, 62

Aug 18-2:52 PM

Aug 18-2:52 PM

Aug 18-2:52 PM



Aug 18-2:52 PM